

# Measuring trends and persistence in capital and labor misallocation

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## Research question

- What is the extent and nature of misallocation of capital and labor in the Dutch economy, and how has it evolved over time?

## Motivation

- Several papers misallocation is a serious problem and has increased since the Great Recession (Gopinath et al., 2017, Dias, 2018, Restuccia and Rogerson, 2017);

## Main contribution

- Extent previous research by analyzing nature, persistence and trends of misallocation.

## Main take-aways from our study

- 1 Misallocation of capital in the Netherlands has increased over the period 2001–2017;
- 2 Misallocation of labor has remained more or less stable in our sample;
- 3 Capital wedge is relatively **large** for small, **highly productive** firms;
- 4 Capital wedge is relatively **small** for (large) **unproductive** firms;
- 5 Misallocation of labor is **temporary** for most firms, and dies out relatively quickly;
- 6 Misallocation of capital is **more permanent**, and the temporary component dies out slowly.

## Raw database

- Population of Dutch firms that declare corporate income tax in period 2001–2017;
- Matched with firm-level data of Dutch business registry;
- Fine grained sectoral division: NACE 5-digit,
- Number of employees (FTE/WP), size-class, balance sheet items, profit & loss account.

## Analyzed database

- Repeated cross-section (highly unbalanced), restricted to non-agricultural non-financial sector;
- “Standard” cleaning (e.g. Gamberoni et al., 2016 and Gopinath et al., 2017);
- Number of observations: 1,831,575;
- Number of firms: 342,245 (+/- 110 thousand p/y)

## Key equations Hsieh and Klenow (2009)

Production function:  $Y_i = TFPQ_i L_i^\alpha K_i^{1-\alpha},$

Profit maximization:  $\pi_i = (1 - \tau_i^Y) P_i Y_i - wL_i - (1 + \tau_i^K) RK_i,$

Profit maximizing price:  $P_i = \frac{\sigma}{\sigma-1} MC_i,$

Marginal costs:  $MC_i = \left(\frac{RK_i}{\alpha}\right)^\alpha \left(\frac{wL_i}{1-\alpha}\right)^{1-\alpha} \frac{(1+\tau_i^K)^\alpha}{TFPQ_i(1-\tau_i^Y)}$

## Note

- “Wedges” on output ( $\tau_i^Y$ ) and capital ( $\tau_i^K$ ) are non-standard elements.
- $TFPQ_i \uparrow \Rightarrow MC_i \downarrow \Rightarrow P_i \downarrow \Rightarrow Y_i \uparrow;$
- $\tau_i^Y \mid \tau_i^K \uparrow \Rightarrow MC_i \uparrow \Rightarrow P_i \uparrow \Rightarrow Y_i \downarrow$

## Misallocation measures Hsieh and Klenow (2009)

Marg. rev. product of labor:  $MRPL_i = (1 - \alpha) \left( \frac{\sigma-1}{\sigma} \right) \left( \frac{P_i Y_i}{L_i} \right) = \left( \frac{1}{1-\tau_i^Y} \right) w,$

Marg. rev. product of capital:  $MRPK_i = \alpha_s \left( \frac{\sigma-1}{\sigma} \right) \left( \frac{P_i Y_i}{K_i} \right) = \left( \frac{1+\tau_i^K}{1-\tau_i^Y} \right) R,$

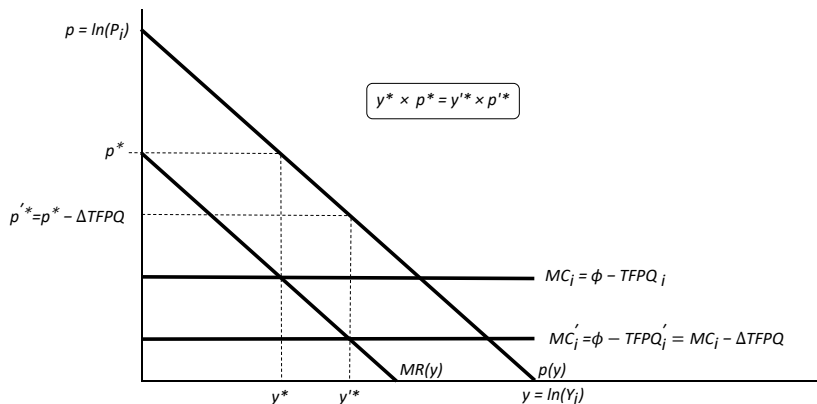
Total rev. factor productivity:  $TFPR_i = P_i TFPQ_i \propto (MRPL_i)^{1-\alpha} (MRPK_i) \propto \frac{(1+\tau_i^K)^\alpha}{1-\tau_i^Y}$

### Note:

- In the absence of distortions  $MRPK_i$  &  $MRPL_i$  would be equated across all firms;
- If  $\text{std}(MRPK) \neq 0 \mid \text{std}(MRPL) \neq 0 \Rightarrow \text{std}(TFPR) \neq 0$ ;
- $\text{Std}(MRPK)$ ,  $\text{std}(MRPL)$ ,  $\tau_i^K$  and  $\tau_i^Y$  our measures of misallocation;

# Hsieh and Klenow (2009) framework: intuition

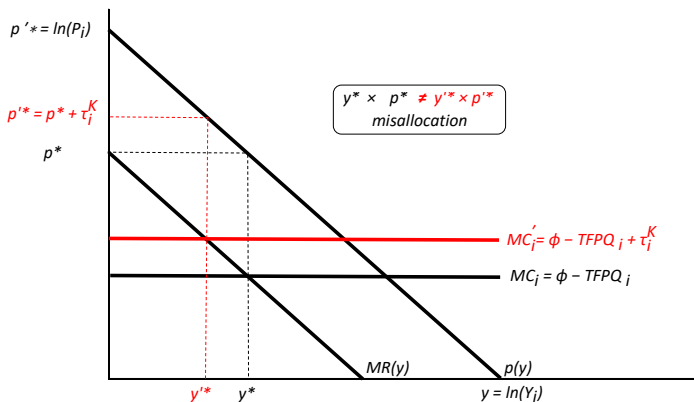
## Effect of a change in $TFPQ$



- All “wedges” are zero
- firms with higher  $TFPQ_i$  produce more at lower price ( $p'^*$ )
- Consequence: economy wide  $TFPQ$  is at efficient level ( $TFPQ_{efficient}$ )

# Hsieh and Klenow (2009) framework: intuition

## Effect of a wedge on capital ( $\tau^K$ )

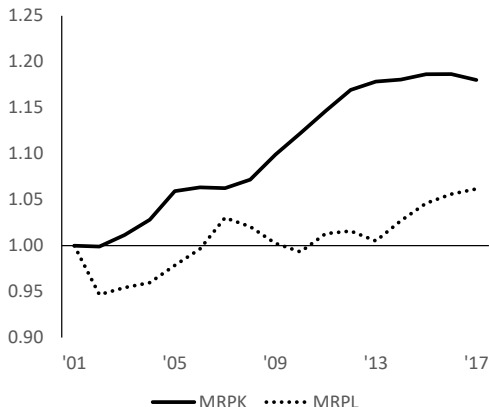


- $\tau^K$  is disturbing allocation,  $TFPR'^* \neq TFPR^* \Rightarrow \text{std}(TFPR) \neq 0$
- Reason:  $p'^*$  is too high and  $y'^*$  is too low given firm's  $TFPQ$
- Consequence: economy wide  $TFPQ$  is lower than  $TFPQ_{\text{efficient}}$



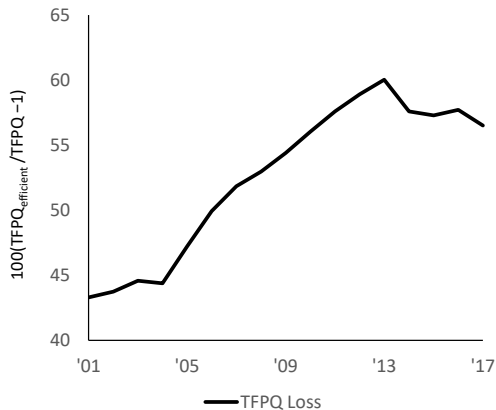
# Outcome: standard deviation $MRPK$ & $MRPL$

Increase  $\text{std}(MRPK) \gg \text{std}(MRPL)$



- $\text{std}(MRPK_{industry}) < \text{std}(MRPK_{services})$
- $\text{std}(MRPK_{large}) < \text{std}(MRPK_{med.}) < \text{std}(MRPK_{small}) < \text{std}(MRPK_{micro})$
- $\text{std}(MRPL_{industry}) < \text{std}(MRPL_{services})$

## Total TFP Loss



- $TFPQ_{efficient} \Rightarrow \text{std}(MRPK) = \text{std}(MRPL) = \text{std}(TFPR) = 0$

## More to misallocation than wedges...

Haltiwanger, Kulick, Syverson (2018), David and Venkateswaran (2019), Bils, Klenow and Ruane (2018)

## Counterfactual analysis: what if only “disturbance” is ...

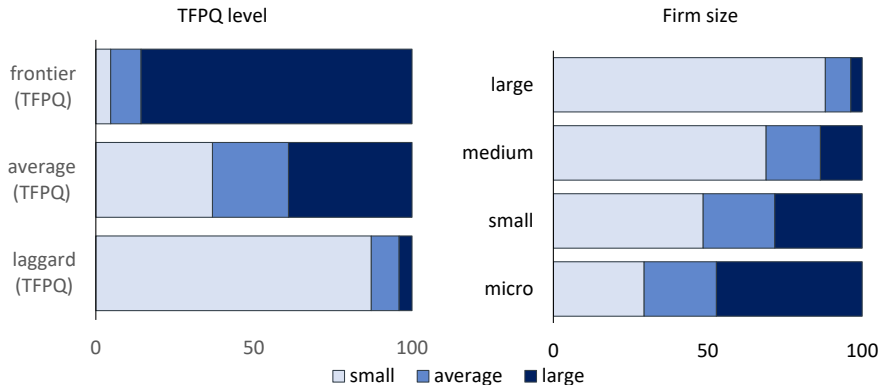
Heterogeneity in production function	1%
Heterogeneous markups	25%
Adjustment costs capital	10%

Large part of our misallocation measure is “true” misallocation

# Nature of misallocation: probability high/average/low wedge

Ordered probit  $\tau_i^K$ : small(decile 1:4) — average(decile 5:7) — large(decile 8:10)

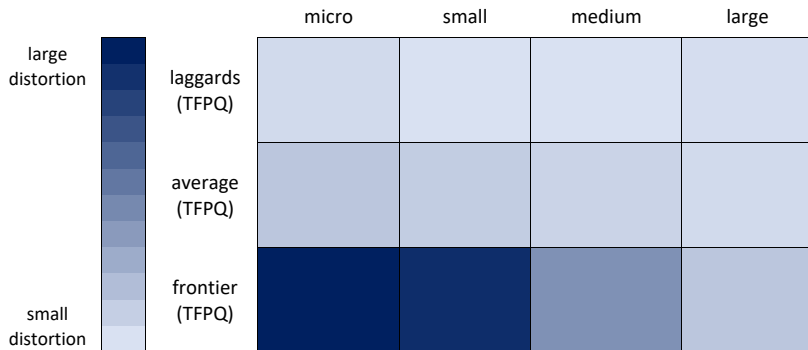
**Regressors:** dummyset TFPQ (frontier/average/laggard), dummyset size-class (micro, small, medium, large), dummyset year (2001–2017), dummyset NACE Rev.2 (2-digit)



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## How persistent is misallocation?

- Exploit empirical specifications from literature on individual earnings (Ng, 2008; Guvenen, 2009, Doris et al., 2013)
- Split  $MRPK/MRPL$  ( $y_{i,t}$ ) in permanent ( $y_{i,t}^P$ ) and transitory ( $y_{i,t}^T$ ) component.

## Formula's Doris et al., 2013

$$y_{i,t} = y_{i,t}^P + y_{i,t}^T$$

$$y_{i,t} = \rho_t \eta_i + \lambda_t v_{i,t}$$

$$v_{i,t} = \rho v_{i,t-1} + \varepsilon_{i,t}$$

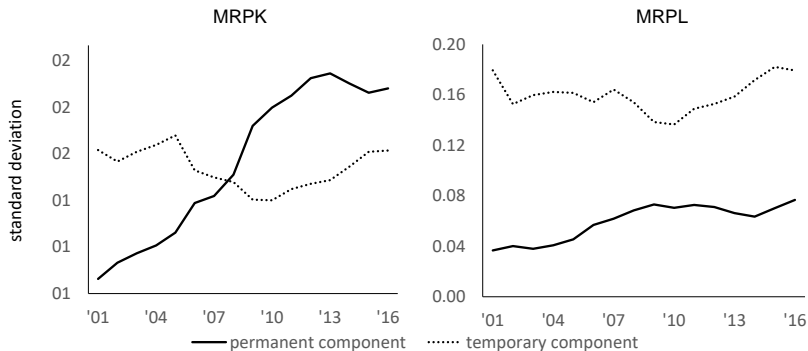
$$V_{t,\infty} = \rho_t^2 \sigma_\eta^2 + \lambda_t^2 \sigma_{v1}^2, \quad t = 1,$$

$$V_{t,\infty} = \rho_t^2 \sigma_\eta^2 + \lambda_t^2 (\rho^{2t-2} \sigma_{v1}^2 + \sigma_\varepsilon^2 \sum_{w=0}^{t-2} \rho^{2w}), \quad t > 1.$$

## Doris et al., 2013 intuition

- General Method of Moments (GMM) estimator;
- Firm-level heterogeneity in permanent component;
- Transitory component is a homogenous AR(1) process.

## Permanent & transitory component MRPK and MRPL



- *MRPK* has become more permanent, *MRPL* mainly transitory;
- $\text{std}(\text{MRPK}_{\text{industry}}^P) < \text{std}(\text{MRPK}_{\text{services}}^P)$
- $\text{std}(\text{MRPK}_{\text{large}}^P) < \text{std}(\text{MRPK}_{\text{med.}}^P) < \text{std}(\text{MRPK}_{\text{small}}^P) < \text{std}(\text{MRPK}_{\text{micro}}^P)$

## Closer look at transitory component...

$$y_{i,t} = \eta_i + v_{i,t}$$

$$v_{i,t} = \rho_i v_{i,t-1} + \varepsilon_{i,t}$$

$$y_{i,t} = (1 - \rho_i)\eta_i + \rho_i y_{i,t-1} + \varepsilon_{i,t}$$

$$y_{i,t} = \alpha_i + \rho_i y_{i,t-1} + \varepsilon_{i,t}$$

## Note:

- Modelling  $\rho_i$  costly in terms of parameters;
- Need to restrict sample: balanced sample 2001–2017;
- OLS estimation;

## Confirms outcome previous model...

- *MRPK*:  $\bar{\rho}_i = 0.59$ , std. = 0.27, skewness = -0.93 (left-skewed)
- *MRPL*:  $\bar{\rho}_i = 0.45$ , std. = 0.30, skewness = -0.06 (symmetric)



## Alternative to permanent and transitory components

- Assume that some firms have a unit root in  $MRPK/MRPL$  while others have not (Ng, 2008);
- $\text{std.}MRPK/MRPL$  will be increasing.

## Approach:

$$V_{t,\infty} = \Lambda_{\infty} + \theta \cdot t + c,$$

$$\hat{\theta} = \frac{1}{T} \sum_{t=1}^T \Delta V_{t,N}$$

## Note:

- $V_{t,\infty}$  = cross-sections variance of  $y_i$ ,  $t$  in period  $t$ ;
- $\Lambda_{\infty}$  = asymptotic cross-sectional average of  $\eta_i$ ;
- $\theta$  = fraction of firms for which  $\rho_i = 1$ .

## Also more persistence in the transitory component of MRPK...

- $\hat{\theta}_{MRPK} = 0.184$ , statistically significant at 1% 18.4% of firms have UR;
- $\hat{\theta}_{MRPL} = 0.063$ , not statistically significant: no UR's.

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